Faculty of Physics, Mathematics and Natural Sciences

1

educational division (faculty/institute/academy) as higher education programme developer

## **COURSE SYLLABUS**

Nonlinear evolution equations

**Recommended by the Didactic Council for the Education Field of:** 

01.04.01 Mathematics

field of studies / speciality code and title

The course instruction is implemented within the professional education programme of higher education:

«Functional methods in differential equations and interdisciplinary research»

higher education programme profile/specialisation title

## 1. COURSE GOAL(s)

The purpose of mastering the discipline "Nonlinear evolution equations" is the teaching of the modern achievements of the theory of evolution partial differential equations with the emphasis on equations of odd orders: properties of function spaces of evolutionary type, the theory of semigroups, and the theory of boundary value problems for the Korteweg-de Vries equation.

## 2. REQUIREMENTS FOR LEARNING OUTCOMES

Mastering the discipline "Nonlinear evolution equations" is aimed at developing the following competencies (parts of competencies):

*Table 2.1. The list of competencies formed by students in the course of mastering the discipline (the results of mastering the discipline)* 

Code	Competence	Competence achievement indicators (within this discipline)	
GC-1	situations based on a	<ul> <li>GC-1.1. Analyzes the problem situation as a system, identifying its components and relationships between them</li> <li>GC-1.2. Identifies gaps in information needed to solve a problem situation and designs processes to address them</li> <li>GC-1.3. Critically evaluates the reliability of information sources, works with conflicting information from different sources</li> <li>GC-1.4. Develops and substantively argues a strategy for solving a problem situation based on a systematic and interdisciplinary approach</li> <li>GC-1.5. Uses logical and methodological tools for a</li> </ul>	
		critical assessment of modern concepts of a philosophical and social nature in his subject area	

### **3.COURSE IN HIGHER EDUCATION PROGRAMME STRUCTURE**

The discipline "Nonlinear evolution equations" refers to the part formed by the participants in the educational relations of block B1 of the EP HE.

As part of the EP HE, students also master other disciplines and / or practices that contribute to the achievement of the planned results of mastering the discipline "Nonlinear evolution equations".

Table 3.1. The list of the higher education programme components/disciplines that contribute to the achievement of the expected learning outcomes as the course study results

Code	Competence	Previous disciplines/modules, practices	Subsequent disciplines/modules, practices*
GC-1	Able to carry out a critical analysis of problem situations based on a systematic	Modern problems of mathematics	State exam

Code	Competence	Previous disciplines/modules, practices	Subsequent disciplines/modules, practices*
	approach, develop an action strategy		

## 4. COURSE WORKLOAD AND ACADEMIC ACTIVITIES

The total labor intensity of the discipline "Nonlinear evolution equations" is 3 credits.

*Table 4.1. Types of academic activities during the periods of higher education programme mastering (full-time training)*\*

Turne of study moult		TOTAL,	Semester			
Type of study work		<b>a</b> .h.	1	2	3	4
Contact academic hours	Contact academic hours				40	
including:						
Lectures (LC)		20			20	
Lab work (LW)						
Seminars (workshops/tutorials) (S)		20			20	
Self-studies		41			41	
<i>Evaluation and assessment (exam/passing/failing grade)</i>		27			27	
Course workload	a.h.	108			108	
	credits	3			3	

### **5. COURSE CONTENTS**

*Table 5.1. Course contents and academic activities types* 

<b>Course Module Title</b>	<b>Brief Description of the Module</b>	Type of study
	Content	work
Section 1. Functional spaces	Topic 1.1. Bochner measurability	Lecture, seminar
of evolutionary type	Topic 1.2. Bochner integral.	
	Topic 1.3. Sobolev spaces.	
Section 2. Semigroups and	Topic 2.1. Theory of semigroups.	Lecture, seminar
groups of operators	Topic 2.2. Theory of groups.	
	Topic 2.3. Abstract initial value problem.	
Section 3. Initial value	Topic 3.1. General properties of solutions.	Lecture, seminar
problem for the Airy	Topic 3.2. Special properties of solutions.	
equation		
Section 4. Initial value	Topic 4.1. Definition and properties of	Lecture, seminar
problem for the Korteweg-	generalized solutions.	
de Vries equation	Topic 4.2. Theorems on existence and	
	uniqueness.	

# 6. CLASSROOM EQUIPMENT AND TECHNOLOGY SUPPORT REQUIREMENTS

Classroom type	Classroom equipment	Specialized educational/laboratory equipment, software and materials for mastering the discipline
Lecture	An auditorium for lecture-type classes, equipped with a set of specialized furniture; board (screen) and technical means of multimedia presentations.	-
Seminar	An auditorium for conducting seminar-type classes, group and individual consultations, current control and intermediate certification, equipped with a set of specialized furniture and technical means for multimedia presentations.	-
For independent work of students	An auditorium for conducting seminar-type classes, group and individual consultations, current control and intermediate certification, equipped with a set of specialized furniture and technical means for multimedia presentations.	-

# 7. RESOURCES RECOMMENDED FOR COURSE STUDY

### Main literature:

- 1. Faminskii A.V. Functional spaces of evolutionary type. 2-d edition. Moscow: RUDN, 2016.
- 2. Faminskii A.V. Selected chapters of the theory of evolution equations. Moscow: RUDN, 2014.

### Additional literature:

- 1. Josida K. Functionsl analysis. Moscow: LKI, 2007.
- 2. Gaevskii H., Greger K., Zakharias K. Nonlinear operator equations and operator differential equations. Moscow: Mir, 1978.

### Resources of the information and telecommunications network "Internet":

1. RUDN ELS and third-party ELS, to which university students have access on the basis of concluded agreements:

- RUDN Electronic Library System RUDN EBS http://lib.rudn.ru/MegaPro/Web
- ELS "University Library Online" http://www.biblioclub.ru
- EBS Yurayt http://www.biblio-online.ru
- ELS "Student Consultant" www.studentlibrary.ru
- EBS "Lan" http://e.lanbook.com/

- EBS "Trinity Bridge"

#### 2. Databases and search engines:

- electronic fund of legal and normative-technical documentation http://docs.cntd.ru/
- Yandex search engine https://www.yandex.ru/
- Google search engine https://www.google.ru/
- abstract database SCOPUS http://www.elsevierscience.ru/products/scopus/

### 8. ASSESSMENT TOOLKIT AND GRADING SYSTEM\* FOR EVALUATION OF STUDENTS' COMPETENCES LEVEL UPON COURSE COMPLETION

Evaluation materials and a point-rating system\* for evaluating the level of formation of competencies (parts of competencies) based on the results of mastering the discipline "Nonlinear evolution equations" are presented in the Appendix to this Work Program of the discipline

## **Developer:**

A.V. Faminskii

signature

name and surname

#### HEAD OF HIGHER EDUCATION PROGRAMME:

V.I. Burenkov

signature

name and surname

## HEAD OF EDUCATIONAL DEPARTMENT A.B. Muravnik

signature

name and surname